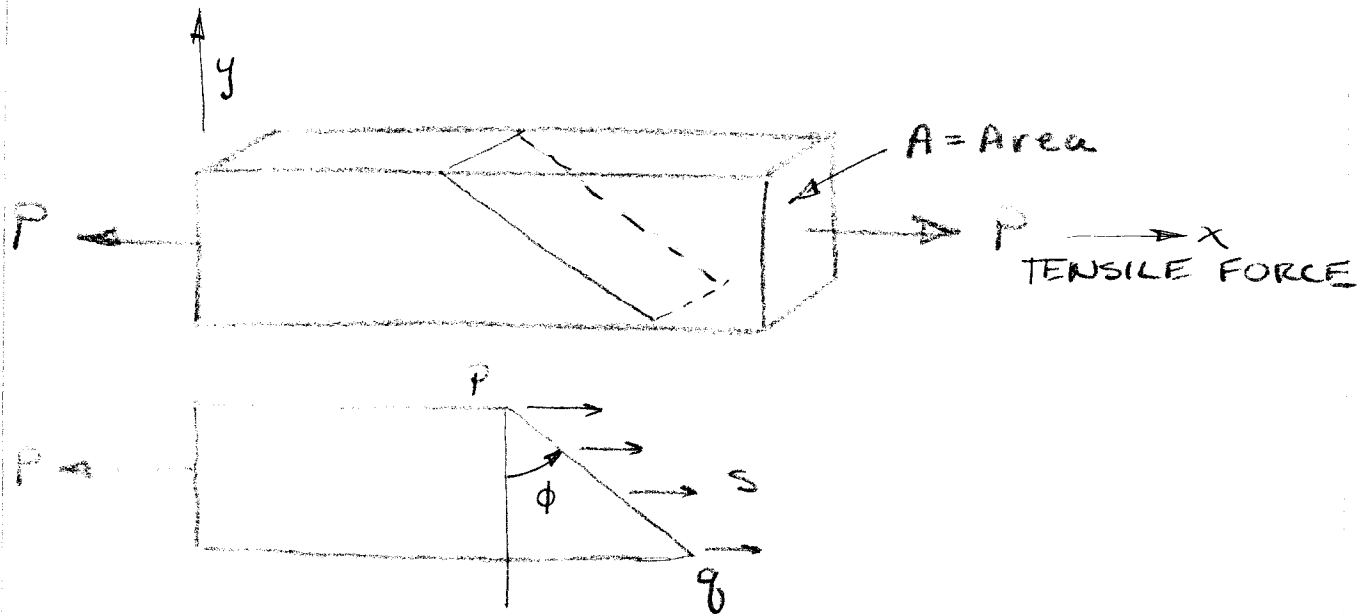


UNIAXIAL STRESS + MOHR'S CIRCLE



$$A \sec \phi = \frac{A}{\cos \phi}$$

S = STRESS OVER $A \sec \phi$

$$S = \frac{P}{A \sec \phi} = \frac{P \cos \phi}{A}$$

STRESS OVER A IS $\sigma_x = \frac{P}{A}$

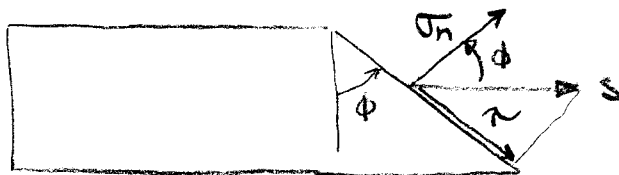
SO

$$(1) \quad S = \sigma_x \cos \phi$$

$$\text{AS } \phi : 0 \rightarrow \frac{\pi}{2}$$

$$\sigma_x : \sigma_x \rightarrow 0$$

CONSIDER COMPONENTS OF S ON $A \sec \phi$



σ_n = normal stress

τ = shear stress

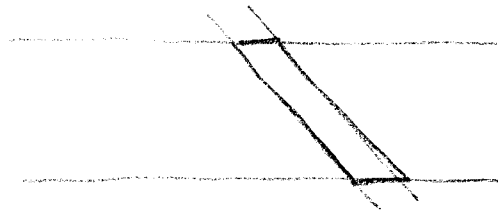
$$\sigma_n = s \cos \phi = \sigma_x \cos^2 \phi$$

$$(2) \quad \tau = s \sin \phi = \sigma_x \cos \phi \sin \phi = \frac{\sigma_x}{2} \sin 2\phi$$


$$\uparrow \quad 0 \rightarrow \tau_{\max} = \frac{\sigma_x}{2} \quad \text{as } \phi \cdot 0 \rightarrow \frac{\pi}{4}$$


Maximum shear stress is 45° to normal stress in uniaxial tension

ELEMENT

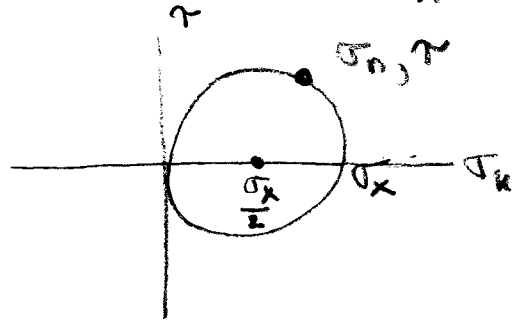


2 MECHANICAL EFFECTS ON PLANAR ELEMENT INCLINED AT ϕ

 extension

 sliding

IF WE PLOT σ_n VS τ ON AXES



(1) and (2) define a circle

MOHR'S CIRCLE

radius $\frac{\sigma_x}{2}$

centered at

$$\frac{\sigma_x}{2}, 0$$

EQ OF CIRCLE

$$(x - a)^2 + y^2 = r^2$$

SUBSTITUTING

$$\left(\sigma_n - \frac{\sigma_x}{2}\right)^2 + \tau^2 = \left(\frac{\sigma_x}{2}\right)^2$$

USING (1) + (2)

$$\cancel{\sigma_x^2 \cos^4 \phi} - \cancel{2 \frac{\sigma_x^2 \cos^2 \phi}{2}} + \cancel{\left(\frac{\sigma_x}{2}\right)^2} + \cancel{\frac{\sigma_x^2 \sin^2(2\phi)}{4}} = \cancel{\left(\frac{\sigma_x}{2}\right)^2}$$

$\uparrow \cos^2 \phi \sin^2 \phi$
 \uparrow

$$\cos^4 \phi - \cos^2 \phi + \cos^2 \phi \sin^2 \phi = 0$$

$$\cos^2 \phi (\cos^2 \phi - 1) + \cos^2 \phi \sin^2 \phi = 0$$

$$\cos^2 \phi (-\sin^2 \phi) + \cos^2 \phi \sin^2 \phi = 0$$

QED